

Graphing Sinusoidal Functions

Sketch the graph of each function for $-2\pi \leq x \leq 2\pi$.

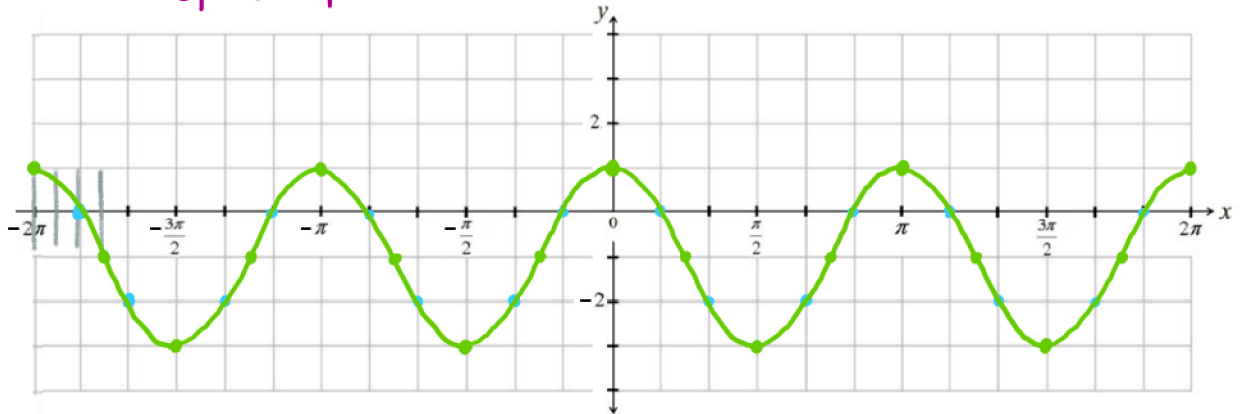
1. $y = 2 \cos(2x) - 1$
positive cosine: start at a max

amplitude: 2

period: $\frac{2\pi}{2} = \pi$

range: $-3 \leq y \leq 1$
 $-2 \leq y \leq -1$

phase shift: none
↳ start on y-axis



negative sine: start on centre line and move down

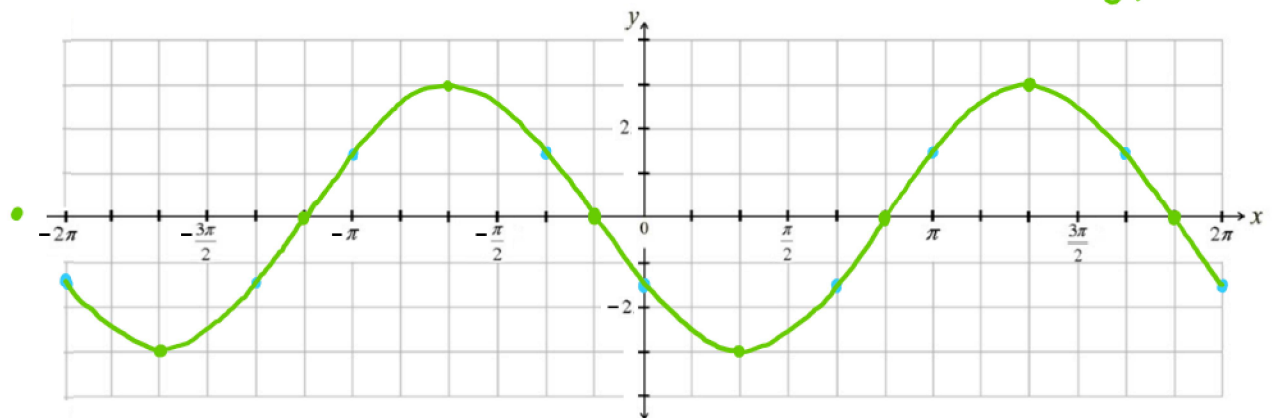
2. $y = -3 \sin\left(x + \frac{\pi}{6}\right)$

amplitude: 3

period: 2π

range: $-3 \leq y \leq 3$

phase shift: $-\frac{\pi}{6}$
↳ starting point



start on centre line and move up

3. $y = \sin\left(2\left(x + \frac{2\pi}{3}\right)\right) + 1$

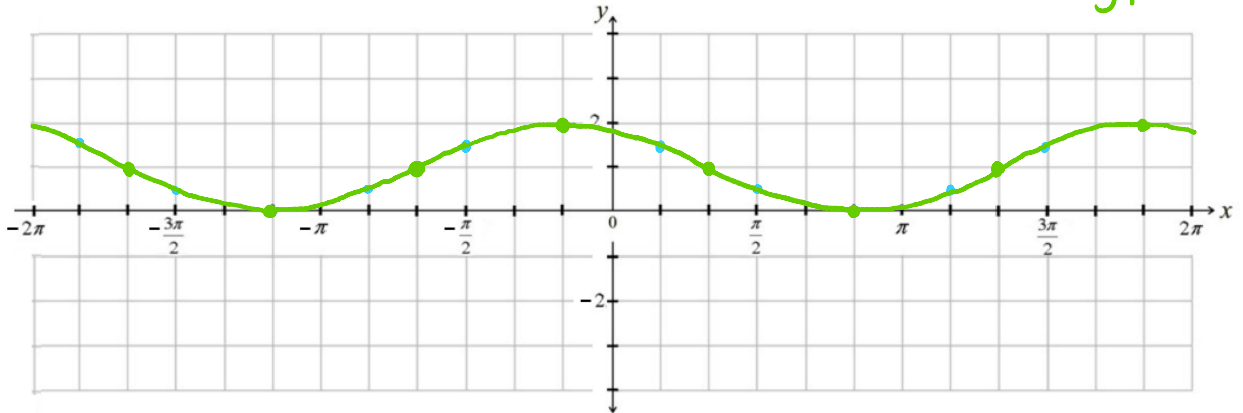
amplitude: 1

period: $\frac{\pi}{2}$

range: $0 \leq y \leq 2$

phase shift: $-\frac{2\pi}{3}$

starting point



negative cosine: start at a min

4. $y = -3 \cos\left(\frac{x}{2} - \frac{\pi}{6}\right) + 1$ *factor the coefficient of x to determine the phase shift

amplitude: 3

period: $\frac{2\pi}{1/2} = 4\pi$

range: $-2 \leq y \leq 4$

phase shift: $\frac{\pi}{3}$

$-3 \leq y \leq 3$
+1 +1

