

3.5 Factoring Trinomials Part II

Math 10

Factoring Trinomials – Part II

Trinomials with a common factor.

$$\begin{aligned}
 &2x^2 + 6x - 20 \\
 &= 2(x^2 + 3x - 10) \\
 &= 2(x^2 + 5x - 2x - 10) \\
 &= 2(x(x+5) - 2(x+5)) \\
 &= 2(x+5)(x-2)
 \end{aligned}$$

$$\begin{aligned}
 &3a^2 - 18a + 24 \\
 &= 3[a^2 - 6a + 8] \\
 &= 3[a^2 - 4a - 2a + 8] \\
 &= 3[a(a-4) - 2(a-4)] \\
 &= 3(a-4)(a-2)
 \end{aligned}$$

$$\begin{aligned}
 &4t^3 - 24t^2 + 20t \\
 &= 4t[t^2 - 6t + 5] \\
 &= 4t[t^2 - 5t - 1t + 5] \\
 &= 4t[t(t-5) - 1(t-5)] \\
 &= 4t(t-5)(t-1)
 \end{aligned}$$

Trinomials with multiple variables.

$$\begin{aligned}
 &x^2 + xy - 30y^2 \\
 &= x^2 + 6xy - 5xy - 30y^2 \\
 &= x(x+6y) - 5y(x+6y) \\
 &= (x+6y)(x-5y)
 \end{aligned}$$

$$\begin{aligned}
 &m^2 - 5mn - 6n^2 \\
 &= m^2 - 6mn + 1mn - 6n^2 \\
 &= m(m-6n) + 1n(m-6n) \\
 &= (m-6n)(m+n)
 \end{aligned}$$


$$\begin{aligned}
 &2p^2 - 14pq + 24q^2 \\
 &= 2[p^2 - 7pq + 12q^2] \\
 &= 2[p^2 - 3pq - 4pq + 12q^2] \\
 &= 2[p(p-3q) - 4q(p-3q)] \\
 &= 2(p-3q)(p-4q)
 \end{aligned}$$

Trinomials of higher degrees.

$$\begin{aligned}
 &a^4 + 2a^2 - 24 \quad \text{let } a^2 = A \\
 &A^2 + 2A - 24 \\
 &= A^2 + 6A - 4A - 24 \\
 &= A(A+6) - 4(A+6) \\
 &= (A+6)(A-4) \\
 &= (a^2+6)(a^2-4)
 \end{aligned}$$

$$\begin{aligned}
 &20 + n^2 - n^4 \\
 &= -n^4 + n^2 + 20 \\
 &= -N^2 + N + 20 \\
 &= -(N^2 - N - 20) \\
 &= -[N^2 - 5N + 4N - 20] \\
 &= -[N(N-5) + 4(N-5)] \\
 &= -(N-5)(N+4) \\
 &= -(n^2-5)(n^2+4)
 \end{aligned}$$

$$\begin{aligned}
 &3d^5 - 6d^3 + 3d \\
 &= 3d[d^4 - 2d^2 + 1] \\
 &= 3d[D^2 - 2D + 1] \\
 &= 3d[D^2 - 1D - 1D + 1] \\
 &= 3d[D(D-1) - 1(D-1)] \\
 &= 3d(D-1)(D-1) \\
 &= 3d(d^2-1)(d^2-1)
 \end{aligned}$$



 these can be factored
 → we will learn how to
 do this in the next lesson

Assignment: handout #2bdfh, 3bdf, 4, 5

